

Solving Equations with Distribution & Like Terms

DEVELOP: Solve each equation by first distributing.

$$1) 5(1 + 5x) = 55$$

$$\begin{array}{r} 5 + 25x = 55 \\ -5 \quad \quad \quad -5 \\ \hline 25x = 50 \end{array}$$

$$\frac{25x}{25} = \frac{50}{25}$$

$$x = 2$$

$$3) 3(-1 + 5r) = 72$$

$$\begin{array}{r} -3 + 15r = 72 \\ +3 \quad \quad \quad +3 \\ \hline 15r = 75 \end{array}$$

$$\frac{15r}{15} = \frac{75}{15}$$

$$r = 5$$

$$5) 5(5b - 5) = 75$$

$$\begin{array}{r} 25b - 25 = 75 \\ +25 \quad \quad +25 \\ \hline 25b = 100 \end{array}$$

$$\frac{25b}{25} = \frac{100}{25}$$

$$b = 4$$

$$7) -72 = 4(2 + 4x)$$

$$\begin{array}{r} -72 = 8 + 16x \\ -8 \quad \quad -8 \\ \hline -80 = 16x \end{array}$$

$$\frac{-80}{16} = \frac{16x}{16}$$

$$-5 = x$$

$$9) 51 = 3(-4v + 5)$$

$$\begin{array}{r} 51 = -12v + 15 \\ -15 \quad \quad -15 \\ \hline 36 = -12v \end{array}$$

$$\frac{36}{-12} = \frac{-12v}{-12}$$

$$-3 = v$$

$$11) -60 = 3(-3n - 5)$$

$$\begin{array}{r} -60 = -9n - 15 \\ +15 \quad \quad +15 \\ \hline -45 = -9n \end{array}$$

$$\frac{-45}{-9} = \frac{-9n}{-9}$$

$$5 = n$$

$$2) 4(2n + 5) = 52$$

$$\begin{array}{r} 8n + 20 = 52 \\ -20 \quad \quad -20 \\ \hline 8n = 32 \end{array}$$

$$\frac{8n}{8} = \frac{32}{8}$$

$$n = 4$$

$$4) 3(4m + 2) = 54$$

$$\begin{array}{r} 12m + 6 = 54 \\ -6 \quad \quad -6 \\ \hline 12m = 48 \end{array}$$

$$\frac{12m}{12} = \frac{48}{12}$$

$$m = 4$$

$$6) 5(3x + 1) = 80$$

$$\begin{array}{r} 15x + 5 = 80 \\ -5 \quad \quad -5 \\ \hline 15x = 75 \end{array}$$

$$\frac{15x}{15} = \frac{75}{15}$$

$$x = 5$$

$$8) -52 = -2(1 - 5n)$$

$$\begin{array}{r} -52 = -2 + 10n \\ +2 \quad \quad +2 \\ \hline -50 = 10n \end{array}$$

$$\frac{-50}{10} = \frac{10n}{10}$$

$$-5 = n$$

$$10) 96 = 4(4 - 5n)$$

$$\begin{array}{r} 96 = 16 - 20n \\ -16 \quad \quad -16 \\ \hline 80 = -20n \end{array}$$

$$\frac{80}{-20} = \frac{-20n}{-20}$$

$$-4 = n$$

$$12) -90 = -5(3 + 5v)$$

$$\begin{array}{r} -90 = -15 - 25v \\ +15 \quad \quad +15 \\ \hline -75 = -25v \end{array}$$

$$\frac{-75}{-25} = \frac{-25v}{-25}$$

$$3 = v$$

DEVELOP: Solve each equation by first collecting like terms.

$$13) -4n + n = -6$$

$$\cancel{-3n} = \cancel{-6}$$
$$\frac{-3n}{-3} = \frac{-6}{-3}$$

$$\boxed{n = 2}$$

$$14) 3x - 5x = 4$$

$$\cancel{-2x} = 4$$
$$\frac{-2x}{-2} = \frac{4}{-2}$$

$$\boxed{x = -2}$$

$$15) 5n + 4 + 1 = -10$$

$$\cancel{5n} + \cancel{5} = -10$$
$$-5 = -5$$

$$\frac{\cancel{5n}}{5} = \frac{-15}{5}$$

$$\boxed{n = -3}$$

$$16) 6 = 2m - 4m$$

$$\frac{6}{-2} = \frac{-2m}{-2}$$

$$\boxed{-3 = m}$$

$$17) 5 = x + 2 + 2$$

$$\cancel{5} = \cancel{x} + \cancel{4}$$
$$-4 = -4$$

$$\boxed{1 = x}$$

$$18) -1 = n + 3 - 3n$$

$$\cancel{-1} = \cancel{-2n} + \cancel{3}$$
$$-3 = -3$$

$$\frac{-4}{-2} = \frac{-2n}{-2}$$

$$\boxed{2 = n}$$

$$19) 4x + 4x = 5x - 6$$

$$\cancel{8x} = \cancel{5x} - 6$$
$$-5x = -5x$$

$$\frac{\cancel{3x}}{3} = \frac{-6}{3}$$

$$\boxed{x = -2}$$

$$20) 3p + 1 = p - 7$$

$$\cancel{3p} - \cancel{p} = -7$$

$$2p + 1 = -7$$

$$\frac{2p}{2} = \frac{-8}{2}$$

$$\boxed{p = -4}$$

$$21) 1 - 4n = -5n + 3$$

$$+5n + 5n$$

$$1 + n = 3$$
$$-1 -1$$

$$\boxed{n = 2}$$

$$22) 7 + 2x = 1 - 4x$$

$$+4x + 4x$$

$$7 + 6x = 1$$
$$-7 -7$$

$$\frac{6x}{6} = \frac{-6}{6}$$

$$\boxed{x = -1}$$

$$23) 5p - 5 = 3p + 5$$

$$\cancel{-3p} - \cancel{3p}$$

$$2p - 5 = 5$$
$$+5 +5$$

$$\frac{2p}{2} = \frac{10}{2}$$

$$\boxed{p = 5}$$

$$24) x - 3 = -4x + 7$$

$$+4x + 4x$$

$$5x - 3 = 7$$
$$+3 +3$$

$$\frac{5x}{5} = \frac{10}{5}$$

$$\boxed{x = 2}$$

CRYPTIC QUIZ

1. Why does Beethoven now spend all his time erasing music?

<u>H</u>	<u>E</u>	<u>I</u>	<u>S</u>	<u>D</u>	<u>E</u>	<u>C</u>	<u>O</u>	<u>M</u>	<u>P</u>	<u>O</u>	<u>S</u>	<u>I</u>	<u>N</u>	<u>G</u>
16	6	-4	10	-3	6	-9	7	20	-5	7	10	-4	3	21

2. What is it called when a sea bird lands on a channel marker?

<u>B</u>	<u>U</u>	<u>O</u>	<u>Y</u>	<u>M</u>	<u>E</u>	<u>E</u>	<u>T</u>	<u>S</u>	<u>G</u>	<u>U</u>	<u>L</u>	<u>L</u>
-36	9	7	-8	20	6	6	-2	10	21	9	11	11

3. How does a tree feel after a hard day at work?

<u>B</u>	<u>U</u>	<u>S</u>	<u>H</u>	<u>E</u>	<u>D</u>
-36	9	10	16	6	-3

TO DECODE THE ANSWERS TO THESE QUESTIONS:

Solve each equation below and find your answer in the code. Each time the solution appears, write the letter of that exercise above it.

$$\textcircled{O} \quad 8u = 3u + 35 \quad \frac{8u - 3u}{5} = \frac{35}{5} \quad \boxed{u=7}$$

$$\textcircled{N} \quad 7y = 33 - 4y \quad \frac{7y + 4y}{11} = \frac{33}{11} \quad \boxed{y=3}$$

$$\textcircled{E} \quad 2x + 48 = 10x \quad \frac{48 - 8x}{8} = \frac{8x}{8} \quad \boxed{x=6}$$

$$\textcircled{T} \quad 5t - 26 = 18t \quad \frac{-26}{-21} = \frac{13t}{13} \quad \boxed{t=-2}$$

$$\textcircled{I} \quad k = 8k + 28 \quad \frac{-7k}{-7} = \frac{28}{-7} \quad \boxed{k=-4}$$

$$\textcircled{G} \quad -30n = -27n - 63 \quad \frac{-3n}{-3} = \frac{-63}{-3} \quad \boxed{n=21}$$

$$\textcircled{H} \quad 4x + 4 = 2x + 36 \quad \frac{2x - 4x}{-2x} = \frac{32}{2} \quad \boxed{x=16}$$

$$\textcircled{D} \quad 9y - 1 = y - 25 \quad \frac{8y}{8} = \frac{-24}{8} \quad \boxed{y=-3}$$

$$\textcircled{P} \quad 14p - 8 = 22 + 20p \quad \frac{-16p}{-16} = \frac{30}{-6} \quad \boxed{p=-5}$$

$$\textcircled{L} \quad z + 81 = 9z - 7 \quad \frac{-8z + 81}{-8} = \frac{9z - 7}{-8} \quad \boxed{z=11}$$

$$\textcircled{Y} \quad 39 - 12w = 7 - 16w \quad \frac{14w}{14} = \frac{-32}{4} \quad \boxed{w=-8}$$

$$\textcircled{C} \quad -15v - 40 = 23 - 8v \quad \frac{-7v}{-7} = \frac{63}{-7} \quad \boxed{v=-9}$$

$$\textcircled{M} \quad 63 - x = 2x + 3 \quad \frac{-3x}{-3} = \frac{60}{-3} \quad \boxed{x=20}$$

$$\textcircled{U} \quad 3n + 46 = 1 + 8n \quad \frac{-5n}{-5} = \frac{-45}{-5} \quad \boxed{n=9}$$

$$\textcircled{B} \quad 12r - 18 = 13r + 18 \quad \frac{-r}{-1} = \frac{36}{-1} \quad \boxed{r=-36}$$

$$\textcircled{S} \quad -x - 1 = x - 21 \quad \frac{-2x}{-2} = \frac{-20}{-2} \quad \boxed{x=10}$$

40 What Were the Headlines After a Midget Fortuneteller Escaped From Jail?

What Were the Headlines After a Midget Fortuneteller Escaped From Jail?



Solve each equation and find your solution below. Cross out the box containing that solution. When you finish, write the letters from the remaining boxes in the spaces at the bottom of the page.

$$\textcircled{1} \quad 3(2x + 5) = 39 \quad \frac{6x}{6} = \frac{24}{6} \quad x = 4$$

$$\textcircled{2} \quad 2(6k - 1) = -38 \quad \frac{12k}{12} = \frac{-36}{12} \quad k = -3$$

$$\textcircled{3} \quad 8(7 - y) = -24 \quad \frac{-8y}{-8} = \frac{-80}{-8} \quad y = 10$$

$$\textcircled{4} \quad -4(8 + 5n) = 8 \quad \frac{-20n}{-20} = \frac{40}{-20} \quad n = -2$$

$$\textcircled{5} \quad 6(3x - 5) - 7x = 25 \quad \frac{18x}{18} - \frac{30}{18} - 7x = \frac{25}{18} \quad x = 5$$

$$\textcircled{6} \quad -2(5 + 6m) + 16 = -90 \quad \frac{-12m}{-12} = \frac{-96}{-12} \quad m = 8$$

$$\textcircled{7} \quad 15(t + 2) + 9t = 6 \quad \frac{24t}{24} = \frac{-24}{24} \quad t = -1$$

$$\textcircled{8} \quad 7w - 3(4w + 8) = 11 \quad \frac{-21w}{-21} - \frac{24}{-21} = \frac{11}{-5} \quad w = -7$$

$$\textcircled{9} \quad 22 - 5(6v - 1) = -63 \quad \frac{-30v}{-30} + \frac{5}{-30} = \frac{-90}{-30} \quad v = 3$$

$$\textcircled{10} \quad 18x - (8x - 7) = 67 \quad \frac{10x}{10} + \frac{7}{10} = \frac{60}{10} \quad x = 6$$

$$\textcircled{11} \quad 8(-2x - 4) + 12 = -52 \quad \frac{-16x}{-16} - \frac{32}{-16} = \frac{-52}{-16} \quad x = 2$$

$$\textcircled{12} \quad 2(9n - 1) + 7(n + 6) = -60 \quad \frac{18n}{18} - \frac{2}{18} + \frac{7n}{18} + \frac{42}{18} = \frac{-60}{18} \quad n = -4$$

$$\textcircled{13} \quad -3(3x + 15) - (10 + x) = 35 \quad \frac{-9x}{-9} - \frac{45}{-9} - \frac{10}{-9} - \frac{x}{-9} = \frac{35}{-9} \quad x = -9$$

$$\textcircled{14} \quad 11(4 - 6y) + 5(13y + 1) = 9 \quad \frac{44}{44} - \frac{60y}{44} + \frac{65y}{44} + \frac{5}{44} = \frac{9}{44} \quad y = 40$$

MID	THE	GET	SHA	RTF	AWA	LLM	AKE	EDI
5	-9	-1	2	40	-3	35	-7	15
TOR	UMA	PRI	UNJ	TLA	SON	AL	RGE	TLE
-2	-14	6	4	-20	3	10	-4	8
S	M	A	L	M	E	D	I	G
C	C	C	C	C	C	C	C	C

OBJECTIVE 4-m: To solve equations containing parentheses.

Solving Equations with Distribution & Like Terms

EXTENDING: Solve each equation by first collecting like terms.

1) $-8 - 5n - 7 = -17 + 1 - 4n - 8$

$$\begin{array}{rcl} -15 - 5n & = & -4n - 24 \\ +5n & & +5n \end{array}$$

$$\begin{array}{rcl} -15 & = & n - 24 \\ +24 & & +24 \end{array}$$

$$\boxed{n = 9}$$

2) $-1 + 8a = 8 - 7 - 6a - 2$

$$\begin{array}{rcl} -1 + 8a & = & -6a - 1 \\ +6a & & +6a \end{array}$$

$$\begin{array}{rcl} 14a & = & -1 \\ +1 & & +1 \end{array}$$

$$\frac{14a}{14} = \frac{0}{14}$$

$$\boxed{a = 0}$$

3) $\frac{1343}{120} - x = \frac{7}{6}x + \frac{15}{4} \times \frac{5}{5} \times 4$

$$\begin{array}{rcl} \frac{1343}{120} - x & = & \frac{7}{6}x + \frac{83}{20} \\ +x & & +x \end{array}$$

$$\begin{array}{rcl} \frac{1343}{120} & = & \frac{13}{6}x + \frac{83}{20} \\ -\frac{83}{20} \times 6 & & -\frac{83}{20} \\ \frac{845}{120} & = & \frac{13}{6}x \\ \frac{13}{6} & & \frac{13}{6} \end{array}$$

$$\boxed{x = 3\frac{1}{4}}$$

5) $\frac{5}{6}n + \frac{8}{5} = \frac{23}{5} + \frac{9}{5}n$

$$\begin{array}{rcl} -\frac{9}{5}n & & -\frac{9}{5}n \\ -\frac{4}{5}n + \frac{8}{5} & = & \frac{23}{5} \\ -\frac{8}{5} & & -\frac{8}{5} \\ -\frac{4}{5}n & = & \frac{15}{5} = 3 \end{array}$$

$$\boxed{n = -3\frac{3}{4}}$$

7) $-5.6x + 4.2x = 12.76 - 3.6x$

$$\begin{array}{rcl} -1.4x & = & 12.76 - 3.6x \\ +3.6x & & +3.6x \end{array}$$

$$\frac{2.2x}{2.2} = \frac{12.76}{2.2}$$

$$\boxed{x = 5.8}$$

4) $\frac{3}{2}b - \frac{5}{2} = -\frac{43}{6} - \frac{5}{2}b$

$$\begin{array}{rcl} +\frac{5}{2}b & & +\frac{5}{2}b \\ \frac{4}{2}b - \frac{5}{2} & = & -\frac{43}{6} \\ +\frac{5}{2} & & +\frac{5}{2} \times 3 \end{array}$$

$$\begin{array}{rcl} -\frac{7}{2}b & = & -\frac{7}{6} \\ \frac{4}{2}b & = & \frac{-28}{6} \end{array}$$

$$\boxed{b = -1\frac{1}{6}}$$

6) $1.1x + 1 = -4.59 - 0.2x$

$$\begin{array}{rcl} +0.2x & & +0.2x \end{array}$$

$$\begin{array}{rcl} 1.3x + 1 & = & -4.59 \\ -1 & & -1 \end{array}$$

$$\boxed{1.3x = -5.59}$$

$$\begin{array}{rcl} 1.3 \cancel{1} 5.59 & & 4.3 \\ -52 & & \\ \hline 39 & & \\ -39 & & \\ \hline 0 & & \end{array}$$

$$\boxed{x = -4.3}$$

8) $1.48 - 4.2v = 1 - 4.8v$

$$\begin{array}{rcl} +4.8v & & +4.8v \end{array}$$

$$\begin{array}{rcl} 1.48 + 0.6v & = & 1 \\ -1.48 & & -1.48 \end{array}$$

$$\boxed{\frac{0.6v}{0.6} = \frac{-0.48}{0.6}}$$

$$\begin{array}{rcl} 0.6 \cancel{1} 0.48 & & 0.8 \\ -48 & & \\ \hline 0 & & \end{array}$$

$$\boxed{v = -0.8}$$

EXTENDING: Solve each equation by first distributing.

$$9) -(1 - 3b) = 8(b + 8)$$

$$-1 + 3b = 8b + 64$$

$$-3b \quad -3b$$

$$-1 = 5b + 64$$

$$-64 \quad -64$$

$$-\frac{65}{5} = \frac{5b}{5}$$

$$\boxed{-13 = b}$$

$$11) \frac{157}{3} = -4\left(\frac{9}{4}x - \frac{1}{3}\right)$$

$$\frac{157}{3} = -9x + \frac{4}{3}$$

$$-\frac{4}{3} \quad -\frac{4}{3}$$

$$\frac{153}{3} = -9x$$

$$\boxed{-5\frac{2}{3} = x}$$

$$13) \frac{329}{200} + \frac{1}{3}b = \frac{7}{4}b + \frac{12}{5}\left(\frac{6}{5}b - 2\right)$$

$$\frac{329}{200} + \frac{1}{3}b = \frac{7}{4}b + \frac{72}{25}b - \frac{24}{5}$$

$$-\frac{1}{3}b \quad -\frac{1}{3}b$$

$$\frac{329}{200} = \frac{1289}{300}b - \frac{24}{5}$$

$$+ \frac{24 \times 40}{5 \times 40} \quad + \frac{24}{5}$$

$$\frac{1289}{200} = \frac{1289}{300}b \quad b \div \frac{1289}{300}$$

$$\frac{72}{25} + \frac{7}{4} - \frac{1}{3}$$

$$= \frac{864}{300} + \frac{525}{300} - \frac{100}{300}$$

$$= \frac{1289}{300}$$

$$\frac{1289}{200} \times \frac{300}{1289} = \frac{3}{2}$$

$$\boxed{b = \frac{3}{2}}$$

$$15) -124 = 5(5n - 4.3)$$

$$-124 = 25n - 21.5$$

$$+21.5 \quad +21.5$$

$$\frac{-102.5}{25} = \frac{25n}{25}$$

$$\boxed{-4.1 = n}$$

$$\begin{array}{r} 124.0 \\ -21.5 \\ \hline 102.5 \end{array} \quad \begin{array}{r} 4.1 \\ -100 \\ \hline -25 \\ 0 \end{array}$$

$$17) -6.68 - 3r = 1.6(r - 1.3)$$

$$-6.68 - 3r = 1.6r - 2.08$$

$$+2.08 \quad +3r \quad +2.08$$

$$\frac{-4.6}{-4.6} = \frac{4.6r}{4.6}$$

$$\boxed{-1 = r}$$

$$10) 3(-1 - 6r) = -3(-2 + 3r)$$

$$-3 - 18r = 6 - 9r$$

$$+18r \quad +18r$$

$$-3 = 6 + 9r$$

$$-6 \quad -6$$

$$\frac{-9}{9} = \frac{9r}{9}$$

$$\boxed{-1 = r}$$

$$12) \frac{105}{2} = -\frac{7}{2}\left(-\frac{13}{5}n - 2\right)$$

$$\frac{105}{2} = \frac{91}{10}n + 1$$

$$-7 \quad -7$$

$$\frac{91}{2} = \frac{91}{10}n$$

$$\frac{91}{10} \quad \frac{91}{10}$$

$$\frac{91}{2} \times \frac{10}{91} = 5$$

$$\boxed{5 = n}$$

$$14) \frac{175}{48} - \frac{5}{3}p = \frac{5}{4}\left(-\frac{13}{4}p + 1\right)$$

$$\frac{175}{48} - \frac{5}{3}p = \frac{-65}{16}p + \frac{5}{4}$$

$$-\frac{175}{48} + \frac{65}{16}p \quad + \frac{65}{16}p - \frac{175}{48}$$

$$\frac{115}{48}p = -\frac{115}{48}$$

$$\frac{115}{48} \quad \frac{115}{48}$$

$$\boxed{p = -1}$$

$$16) 54.02 = 3.7(2.9 - 3.9n)$$

$$54.02 = 10.73 - 14.43n$$

$$-10.73 \quad -10.73$$

$$\frac{43.29}{-14.43} = \frac{-14.43n}{-14.43}$$

$$\boxed{-3 = n}$$

$$\begin{array}{r} 3.7 \\ \times 2.9 \\ \hline 33.3 \end{array} \quad \begin{array}{r} 3.7 \\ \times 3.9 \\ \hline 33.3 \end{array}$$

$$\begin{array}{r} 10.73 \\ + 740 \\ \hline 1110 \end{array} \quad \begin{array}{r} 10.73 \\ + 1110 \\ \hline 14.43 \end{array}$$

$$\begin{array}{r} 54.02 \\ - 10.73 \\ \hline 43.29 \end{array} \quad \begin{array}{r} 14.43 \\ - 14.43 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 3.7 \\ \times 3.9 \\ \hline 14.43 \end{array} \quad \begin{array}{r} 3.7 \\ \times 3.9 \\ \hline 14.43 \end{array}$$

$$\begin{array}{r} 10.73 \\ + 4329 \\ \hline 4329 \end{array} \quad \begin{array}{r} 10.73 \\ + 4329 \\ \hline 0 \end{array}$$

$$18) -9.27 + 2.8k = 3.9(k - 1.7)$$

$$-9.27 + 2.8k = 3.9k - 6.63$$

$$+6.63 - 2.8k \quad -2.8k + 6.63$$

$$+390 \quad +390$$

$$\frac{-2.64}{1.1} = \frac{1.1k}{1.1}$$

$$\boxed{-2.4 = k}$$

$$\begin{array}{r} 3.9 \\ \times 1.7 \\ \hline 273 \end{array} \quad \begin{array}{r} 3.9 \\ \times 1.7 \\ \hline 273 \end{array}$$

$$\begin{array}{r} 10.73 \\ + 273 \\ \hline 380 \end{array} \quad \begin{array}{r} 10.73 \\ + 273 \\ \hline 380 \end{array}$$

$$\begin{array}{r} 54.02 \\ - 380 \\ \hline 16.02 \end{array} \quad \begin{array}{r} 54.02 \\ - 380 \\ \hline 16.02 \end{array}$$

$$\begin{array}{r} 10.73 \\ + 16.02 \\ \hline 26.75 \end{array} \quad \begin{array}{r} 10.73 \\ + 16.02 \\ \hline 26.75 \end{array}$$

$$\begin{array}{r} 10.73 \\ + 26.75 \\ \hline 37.48 \end{array} \quad \begin{array}{r} 10.73 \\ + 26.75 \\ \hline 37.48 \end{array}$$

$$\begin{array}{r} 54.02 \\ - 37.48 \\ \hline 6.54 \end{array} \quad \begin{array}{r} 54.02 \\ - 37.48 \\ \hline 6.54 \end{array}$$

$$\begin{array}{r} 10.73 \\ + 6.54 \\ \hline 17.27 \end{array} \quad \begin{array}{r} 10.73 \\ + 6.54 \\ \hline 17.27 \end{array}$$